Evaluating the Casual Reasoning Abilities of Large Language Models

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Abstract

Large language models have developed at a breathtaking pace, quickly advancing in their ability to generate, summarize, and work with long and short-form text. As these advances become further integrated into society, however, it becomes necessary to question and evaluate how well these models are actually capable of true reasoning, rather than simply mimicking their large training corpora. We argue that eliciting reasoning from language models is the new "explainability method" and introduce CReDETS, a novel and first-of-its-kind causal reasoning dataset with annotated hand-written explanations. We benchmark the latest and most powerful generation of transformer neural network models GPT-3, GPT-3.5 (chatGPT), and GPT-4 and discuss their accuracy, coherence, and consistency. Our staggering results show that even the most recent LLMs have stark weaknesses in reasoning ability that must be ameliorated before they can be integrated with public-facing applications worldwide.

1. Introduction

1.1. The State of New Models

In recent times, Large Language Models have taken much of the public by storm, with their abilities rapidly advancing to include text generation, summarization, question answering, and much more. ChatGPT [16] and GPT4 [15] have skyrocketed in use to become the fastest-growing technology products of all time [5], and they created significant partnerships with industry players, including Microsoft Bing [2], Duolingo [13], Instacart [11], Snapchat [14], and countless other products that put them face to face with customers. The outputs of these models come face to face with vulnerable populations [7] and are often responsible for critical decision-making processes. Some of the notable advances associated with these models include Few-shot Learning, Improved Language Modeling, Enhanced Zero-shot Learning, Context-aware Conversational AI, Knowledge Retrieval and Reasoning, and Transfer Learning. Despite their impressive abilities, however, Large Language Models suffer from several behaviors that can prove dangerous to users treating them as "oracles" and suggest that any "reasoning" demonstrated by the models is not genuine and simply an unreliable mimicry of large-scale training data. As these models are being integrated into impactful parts of society, it is thus urgent that we gain insight into the step-by-step "reasoning processes" taken by LLMs to arrive at their outputs.

1.2. The Disconnect Between Current Explainability Methods and LLMs

A 2017 survey by Chakraborty et al. [4] suggests that *explainability* refers to a complete output, where a model response is accompanied by all relevant parts of the input used for the reasoning behind its decision, while *interpretability* refers to the quality of an explanation based on how a human interprets it, but as is common in practice and literature, we will use the terms mostly interchangeably.

Still, we must recognize that even Chakraborty's definition of explainability proves hard to apply to large language models.

Post-hoc explainability methods, which aim to provide interpretability for model predictions after they have been generated, often struggle to provide effective explanations for large language models like GPT-3.5. There are several key reasons for this:

Complexity and non-linearity: Large language models like GPT-3.5 are composed of millions or even billions of parameters, making them highly complex and non-linear [18]. This complexity makes it difficult for post-hoc explainability methods to meaningfully disentangle the relationships between input features and model predictions. Many traditional methods, such as LIME [19] or SHAP [12], rely on locally linear approximations, which may not adequately capture the intricate relationships learned by large language models.

• Input representation: Large language models use sub-

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word tokenization techniques to represent text inputs. This leads to variable-length input representations depending on the tokens present in the input text. Posthoc explainability methods, which typically assume fixed-length feature spaces, may struggle to adapt to such variable-length input representations.

• Self-attention mechanisms: Transformer architectures, which underpin models like GPT-3.5, rely heavily on self-attention mechanisms to capture long-range dependencies in the input text [22] These self-attention mechanisms enable the model to weight different parts of the input differently, making the relationship between input and output even more complex. This complexity make it difficult to disentangle and interpret the individual contributions of each parameter to the model's output [1]

Above all else, it is *necessary* to shift the paradigm of explainability when considering Large Language Models because of one simple fact - everyday users of LLMs such as GPT3.5 and GPT4 do not have access to the inner workings of the architecture. Even if we were able to develop post-hoc explanation tools that worked on LLMs such as GPT4, normal users of the product only have access to an API output. With nothing but access to an input and an output of the AI model, we argue we must shift the way we think about aiming for explainability with the arrival of LLMs and arguably higly sophisticated intelligent models [3].

2. A new paradigm for "Explainability" -Reasoning in Language Models

We argue that explainability in language models is about extracting *reasoning* from the model, whether through prompting [6], one shot [21]/few shot learning [17], etc. Reasoning is a cognitive process that involves drawing conclusions based on available information, often through logical steps or inferences. By focusing on eliciting the model's reasoning, we can better understand how a model processes and manipulates information to arrive at its conclusions. This approach allows us to extract insights into the model's internal decision-making processes, thus enabling a deeper understanding of the model's behavior.

In order to fully trust that the reasoning a LLM outputs for a given prompt can be used as evidence for its true internal workings, however, we need to have faith in the reasoning abilities of language models. We need to measure how well LLMs can explain their "thinking" - how accurate is their reasoning?

Kojima et al. [9] suggests that simply appending the phrase "Let's think step by step" to any GPT3 prompt induces the model into provide more accurate answers and include the context it uses to extract more accurate answers. OpenAI has claimed, however, that with the arrival of GPT3.5 (Chat-GPT) and GPT4 also comes advanced reasoning abilities and a lesser need to engineer prompts to "elicit" reasoning.

In this paper, we present a thorough analysis of such claims and present a new dataset CReDETS and metrics to measure explaination and reasoning ability of these models.

3. Introduction to CReDETS

Although there are datasets such as LogiQA [10] for measuring general logic abilities of large language models through open ended question and answering benchmarks, there is lack of data sources that explicitly focus on complex causal reasoning Q&A *and* include high quality explanations of those answers as well.

To this end, we introduce CReDETS, the Causal **RE**asoning **D**ataset and **E**xplanation **T**est **S**uite, a novel, first-of-its-kind causal reasoning dataset with hand-annotated explanations. We hope that the introduction of this dataset will allow researchers to continue to evaluate and improve the reasoning abilities of various generations of language models.

In aiming to select questions that would best capture a model's causal reasoning ability, we analyzed several professional and standardized exams and decided upon the Law School Admissions Test (LSAT). The LSAT is one of the only professional tests that doesn't require any subject matter knowledge, and thus is a perfect basis for a causal reasoning dataset. These professional exam questions are written by philosophy and logic experts to specifically measure causal reasoning ability.

We curated 442 samples from the Logic Games section of the LSAT, a section that we specifically chose because of its completely self-contained nature (no external information is required to solve each question) and explicit focus on causal reasoning. As shown in Figure 1, each question is based on a premise involving a set of characters and rules that define relationships between them.

For each question, we include not only the question, answer choices, and correct answer, but also a *hand-written explanation* for each question, a unique differentiation of our dataset with respect to all others in the field such a LogiQA [10].

CReDETS enables the measurement of both causal reasoning accuracy *and* explanation with questions that are pre-vetted by law and philosophy experts, completely self contained, and meant to be solved in quick time periods. It is a first-of-its-kind dataset that includes human-annotated explanations for each causal reasoning question and answer pair. This tests the capabilities of language models

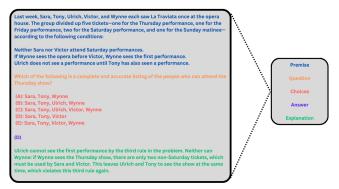


Figure 1. Structure of LSAT Logic Games Questions

to not just choose the right answer options (MCQ) but also to explain reasoning for each question.

3.1. Sourcing and Structure of CreDeTS

We hand-curated and processed 442 questions from a variety of online sources, including Varsity Tutors [20]. The questions and their corresponding explanations are written and vetted by professors and law school admissions professionals around the country. Each question was analyzed and categorized into one of 5 problem types: Grouping, Sequencing, Four/Five Variable, Three Variable, and Two Variable. The distribution of problem types in the preliminary dataset is shown in Figure 2 below.

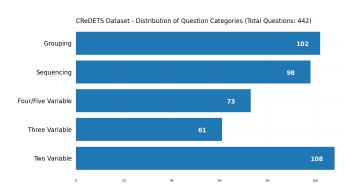


Figure 2. CReDETS Dataset - Distribution of Question Categories (Total Questions: 442)

Each sample was separated into a premise, question, set of answer choices, correct answer, and explanation, organized into a JSON file structure as shown in Figure 3.

Further examples can be found in the appendix.



Figure 3. Example JSON Entry - CReDETS Dataset

4. LLM Results on CReDETS

The CReDETS dataset is a novel, first-of-its-kind dataset that allows us to benchmark both causal reasoning ability *and* ability to explain a model's reasoning. In order to see some real life results on CReDETS, we ran 10 trials of the 442 questions in the preliminary dataset. Questions were tested on GPT 3, 3.5, and 4 via API calls. In this section, we show some examples of our results, discuss their accuracy and consistency, analyze common errors found in the generated text, and discuss the implications of our results.

4.1. Examples

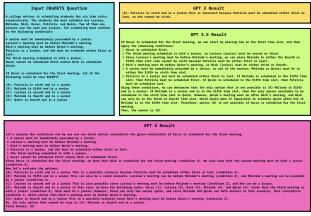


Figure 4. A question sampled from the CReDETS dataset and the responses of GPT 3, GPT 3.5, and GPT 4.

4.2. Accuracy

In order to measure the accuracy of our three test models - GPT3, GPT3.5, and GPT4 - on the questions in the CRe-DETS dataset, we ran 10 trials of the 442 questions. Each question was run via a separate API call. The results can be seen in table 1 below.

Table 1. Test accuracies of GPT3, GPT3.5, and GPT4 on the questions in preliminary CReDETS Dataset. Each trial of 442 questions was run 10 times to measure consistency and average accuracy.

	Model		
	GPT 3	GPT 3.5	GPT 4
Trial Average	0.198	0.207	0.248
Trial 1	.199	.205	.278
Trial 2	.201	.210	.282
Trial 3	.192	.212	.291
Trial 4	.196	.203	.271
Trial 5	.208	.213	.269
Trial 6	.205	.210	.264
Trial 7	.199	.201	.280
Trial 8	.199	.199	.271
Trial 9	.187	.208	.273
Trial 10	.196	.212	.271

As we see in Table 1, all three models (GPT3, GPT3.5, GPT4) perform quite poorly on the CReDETS benchmark. GPT 3 and GPT 3.5 display accuracies close to 0.2 (.198 and .207, respectively), which is quite close to a 0.2 random chance decision, given that there are 5 multiple choice answers. These models also perform quite erratically - as we will discuss later, running each question several times yielded several different answers. While these differences mostly averaged out over all 10 trials and 442 questions, we can still see the inconsistency of these models in the accuracy numbers (in the table and visually displayed in Figure 5).

GPT 4's performance is an improvement to its predecessors - it correctly answers on average 1 in 4 questions, which, while not at all close to human-level accuracy, is a marked improvement from the 1-in-5 accuracy of GPT 3 and GPT 3.5. Most importantly, GPT 4 displays increased levels of consistency - running the same question multiple times results in the same one (or two) answers, which we can see by the general similarity and smoothness of the accuracies in the GPT 4 column of Table 1 and the increased smoothness of the GPT 4 results in Figure 5. We will elaborate on this consistency in Section 4.3.

4.3. Consistency

When it comes to using reasoning ability as a conduit to elicit reasoning from large language models, it is crucial that there is some consistency in the text results they generate. If we run the same question 5 different times, will we get five different answers? Even if we get the same (correct or incorrect) answer, are the steps the model takes to get to the final answer similar? If the model lacks this consistency, it is difficult to trust that any model output can be used as a Accuracy of GPT3, GPT3.5, and GPT4 on CReDETS over 10 Trials

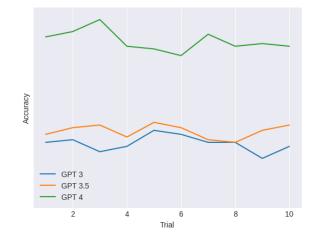


Figure 5. Test accuracies of GPT3, GPT3.5, and GPT4 on the 442 questions in preliminary CReDETS Dataset over 10 trials.

tool to "explain" the model's "decision making".

As we can see in Table 1, the number of questions that GPT 3 and GPT 3.5 answer correctly over the 10 trials varies more than the number of questions that GPT 4 answers correctly. This suggests that GPT 4 is significantly more consistent in its results than GPT 3 and GPT 3.5, even if the results are incorrect.

To analyze this further, we make a plot of the average number of distinct final answer choices made over the 10 trials by each of our three models. (If, for example, over 10 trials on a question, my model answered (A), (B), (C), (C), (B), (A), (A), (C), (B), (C), the number of distinct final answer choices would be 3).

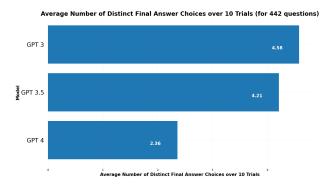


Figure 6. Average Number of Distinct Final Answer Choices Made Over 10 Trials by GPT 3, GPT 3.5, and GPT 4

As we can see in Figure 6, GPT 4 displays a great deal higher consistency than GPT 3 and 3.5. When we run a question 10 times, it usually outputs the same answer, even if that answer is incorrect. When the final generated answer

choice is incorrect, manual analysis shows that the mistakes made by the model are similar in almost all of the generated ouptuts. This consistency in GPT 4 bodes well for our ability to truly use generated reasoning output to interpret the decision-making process of GPT 4, lending some sense of "interpretability" to these outputs.

5. Error Analysis

We hand-analyze the results outputted by GPT3, GPT3.5, and GPT4 on the same, randomly selected set of 25 questions. We found that there were three main categories of errors made by the model. We describe them below.

Factual error relating to problem premise. For example, if the premise of a question states that at most two people can be on a dance committee, and the model output places 4 people on a dance committee, this error would be classified as "factual" due to its misunderstandings of facts stated in the premise of the question. An example is shown below in Figure 7, where the premise of the question clearly states that there are there are two tickets for the Saturday performance, but the GPT-generated result starts by stating that only one person can attend each show, which is factually incorrect.





Causality Error. These errors occur when the model makes decisions based on incorrect causality statements. If the problem premise states that A always comes after B, and the model suggests a situation in which A comes before B, we would register a Causality error. An example is shown below in Figure 8. The text colored in red displays a causality error because there are several statements made that do not causally follow from the rules provided in the question. The model says the following: "Since D is already served on Tuesday or Wednesday with free wine, C cannot be served on Tuesday or Wednesday." The premise of the question states that "free wine is served only on Tuesday or Wednesday." The premise of the question does not imply

that just because D is served on Tuesday or Wednesday with free wine, C *cannot* be served on Tuesday or Wednesday. This is a causality error.

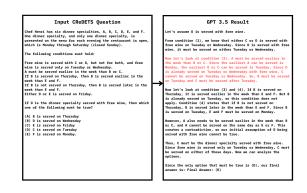


Figure 8. The text colored in red displays a Causality Error.

Self Contradiction. The outputs of LLMs (especially more recent ones, such as GPT4) when given reasoning problems are usually lengthy statements. Oftentimes, these models will make a statement in their output that directly contradicts something that was previously generated. We categorize these errors as "self-contradictory". Figure 9 shows an example with several self-contradiction errors. In the text colored purple, we can see that the explanation says that peppers are on a later pizza than sausage, but the answer it gives is not on a later pizza than sausage. The text highlighted in red outputs an answer choice that pairs sausage and anchovies as well as peppers and bacon, but the choice is rejected because the anchovies cannot be paired with peppers, a pairing that was never outputted. The text highlighted green says includes an explanation that sausage and bacon are on the last pizza, which is contradictory to the answer choice the model outputted. Lastly, the text highlighted in orange mentions that only choices (B) and (E) work, but the model previously outputted that choice (D) worked as well, so this statement is self-contradictory as well.

We randomly sample 25 questions from the CREDETS dataset and manually analyze results produced by GPT 3, GPT 3.5, and GPT 4. We categorize errors made by the model into the following groups: factual errors, causality errors, and self-contradiction errors. The distribution of errors is shown in Figure 10 below.

We can see in the figure that all three models have a large tendency to make causality errors (even GPT 4, despite its higher accuracy and consistency). GPT 4 makes less factual errors than its predecessors, but it has high rates of selfcontradiction, a stark reminder that despite language models

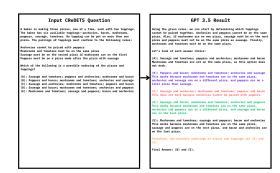


Figure 9. The text colored in purple, red, green, and orange display Self Contradiction Errors.

Total Number of Factual, Causality, and Self Contradiction Errors Outputted by GPT 3, 3.5, and 4

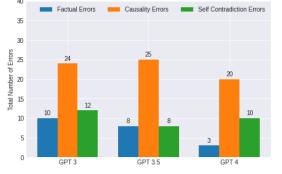


Figure 10. Average Number of Distinct Final Answer Choices Made Over 10 Trials by GPT 3, GPT 3.5, and GPT 4

achieving prolific results, they are still probabilistic algorithms that output their results word by word, as opposed to a more big-ideas / long term reasoning framework that humans use.

Interestingly, the causality errors made by GPT 4 were more likely than those made by its predecessors to belong to an output that resulted in an incorrect final answer. As we can see in Table 2 below, out of the 25 asked questions, GPT 3 incorrectly answered 21 questions, GPT 3.5 incorrectly answered 20, and GPT 4 incorrectly answered 18. The number of Causality Errors made in outputs that resulted in the correct final answer, however, decreased in GPT 4's output, another sign that there is a higher probability that we can trust the reasoning output of GPT 4 to be a form of interpretability for the model's decisions. Table 2. Causality Errors made by GPT 3, 3.5, and 4 in outputs that generated the wrong final answer versus outputs that generated the correct final answer. Manually tabulated over 25 questions.

		Causanty Errors		
	Incorrect Answers	in Correct Answers	in Incorrect Answers	Total Causality Errors
GPT 3	21	3	21	24
GPT 3.5	20	3	22	25
GPT 4	18	1	19	20

6. Discussion

Our results on the preliminary CReDETS dataset show that while cutting-edge models such as GPT 4 display impressive, coherent language modeling abilities, they have a long way to go before coming close to reaching human-ability levels of reasoning.

All three models show poor accuracies on the CReDETS reasoning benchmark questions - with each question having 5 multiple choice answer possibilities, GPT 3, GPT 3.5, and GPT 4 displayed average accuracies of .20, .21, and .25 respectively.

Earlier models, especially GPT 3 and occasionally GPT 3.5, prove to be inconsistent, often generating distinct final answer choices if run on the same problem many times, though this problem is significantly ameliorated in GPT 4.

Outputs by all three language models are riddled with selfcontradictions and factual errors, a fact which reminds us that despite their prowess and size, Large Language Models are in fact just that - models. They compose an output by statistically predicting one word at a time - true reasoning, however, involves thinking several steps ahead and making logical decisions by concept instead of on a word-by-word basis. The high rate of causality errors shown by the GPT models reinforces this notion and makes clear the need for work evaluating how LLMs can improve their base causal reasoning ability.

At this stage, our results show that it is difficult to claim that even today's most powerful language models are capable of true reasoning. Our results showed generated text that was riddled with self-contradictions, causality errors, hallucinations, factual errors, and several other mistakes that suggest that large language models are likely simply parroting their powerfully large training corpora. Major improvements need to be made before we can recognize their abilities as true reasoning, and as LLMs are integrated deeper into our society, great care needs to be taken to ensure that false abilities of "reasoning" do not result in dangerous mistakes or implications.

When thinking about how reasoning can be useful in our paradigm of explainability, it is interesting to note how our results have improved as we test GPT 3, 3.5, and 4. The accuracy, though low for all three models, improved as the parameter size increased. The coherency and intricacy of

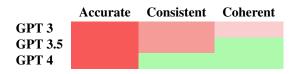


Table 3. Visual depiction of the Accuracy, Consistency, and Coherency of GPT 3, 3.5, and 4 on the CREDETS dataset

produced output improved significantly from GPT 3 to GPT 3.5 to GPT 4. The consistency of the models also improved significantly as the number of parameters increased.

These Large Language Models have shown remarkable improvement and give credence to the hypothesis [8] that increasing the number of model parameters will lead to more accurate modeling of human language.

This improvement in coherency and consistency that GPT 4 has shown demonstrates the possibility that the reasoning steps outputted by the model actually provide a correct, reasonable explanation of an internal "decision process". (In GPT 3, for instance, there were several questions where the model happened to get a correct final answer but the reasoning steps outputted had causal, factual, and self-contradiction errors. In this case, we cannot take the outputted reasoning steps to provide any semblance of interpretability.) As we continue to explore how to derive a sense of explainability from language models where, for the most part, we only have access to an input and output (API call), the improved results displayed by GPT 4 suggest that the reasoning steps outputted by a model could perhaps, in the future, be used as a source of interpretability.

It is our hope that the novel CReDETS dataset, with its unique combination of hand-written explanations and questions designed explicitly to test reasoning ability, will allow researchers to continue to study and evaluate the evolving reasoning abilities of language models.

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A. CReDETS Dataset Examples

Below, we include some further examples of data points from the CReDETS dataset.



Figure 11. Example JSON Entry - CReDETS Dataset

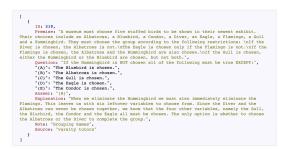


Figure 12. Example JSON Entry - CReDETS Dataset



Figure 13. Example JSON Entry - CReDETS Dataset



Figure 14. Example JSON Entry - CReDETS Dataset